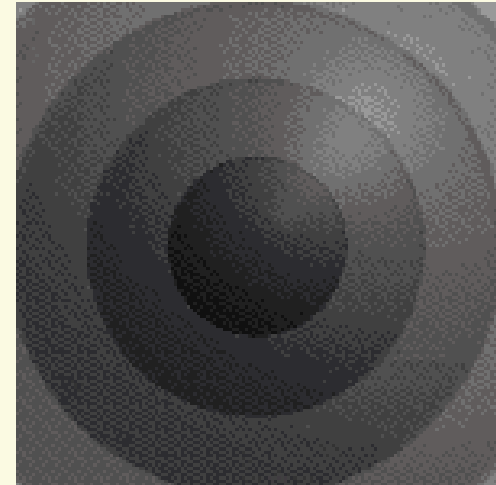
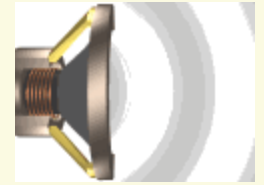


Aula 21: Mecânica Ondulatória

1. Função de onda associada
2. Equação de Schrödinger
3. Difracção de electrões
4. Princípio de Heisenberg
5. Probabilidade de localização



Simulação: função de onda do electrão

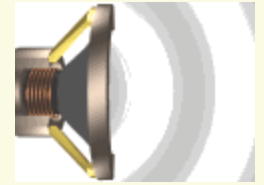


1. Função de onda associada

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

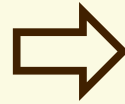
$$\hbar\omega = \frac{mv^2}{2} + \text{const}$$

$$\Psi = A \text{sen}(kx - \omega t) = A \text{sen}\left(\frac{p}{\hbar}x - \frac{E}{\hbar}t\right)$$



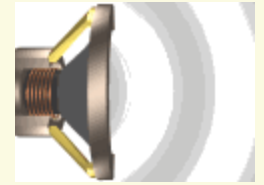
2. Equação de Schrödinger

$$\frac{\partial^2 \Psi}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 \Psi}{\partial t^2}$$



$$\frac{\partial^2 \Psi}{\partial x^2} + \frac{2m}{\hbar^2} (E - U) \Psi = 0$$

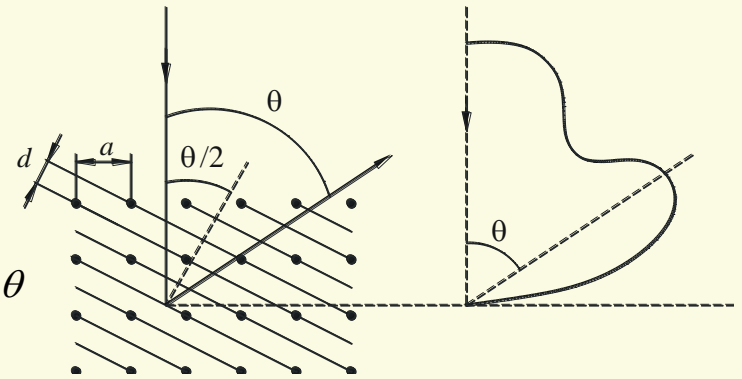
Simulação: difracção de electrões

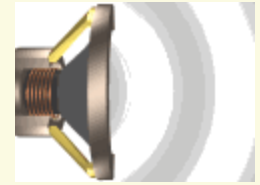


3. Difracção de electrões

$$\lambda = \frac{h}{\sqrt{2m_e \varepsilon}} = \frac{h}{\sqrt{2m_e eV}} = \sqrt{\frac{1.5}{V}} \quad (\text{nm})$$

$$m\lambda = 2 \frac{d}{\cos(\theta/2)} - 2d \tan\left(\frac{\theta}{2}\right) \sin\left(\frac{\theta}{2}\right) = 2d \cos\left(\frac{\theta}{2}\right) = a \sin \theta$$

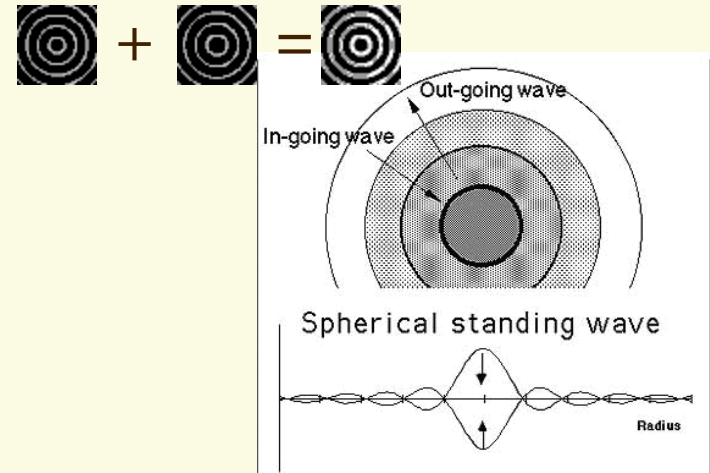
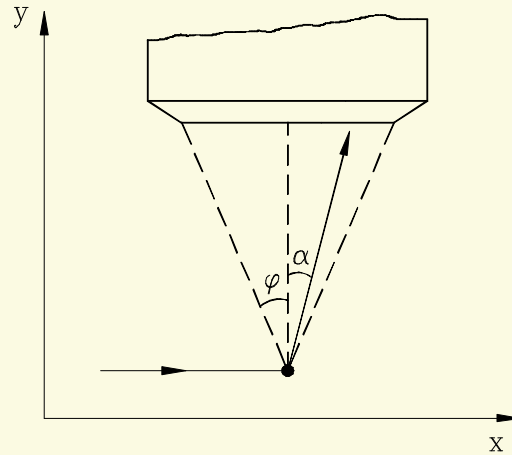




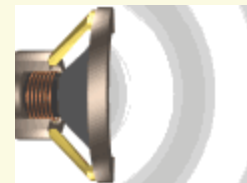
4. Princípio de Heisenberg

$$\Delta x \Delta p_x \geq \frac{\hbar}{2}$$

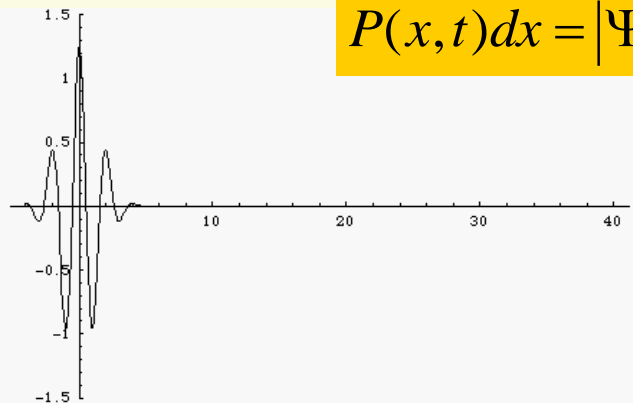
$$\Delta E \Delta t \geq \frac{\hbar}{2}$$



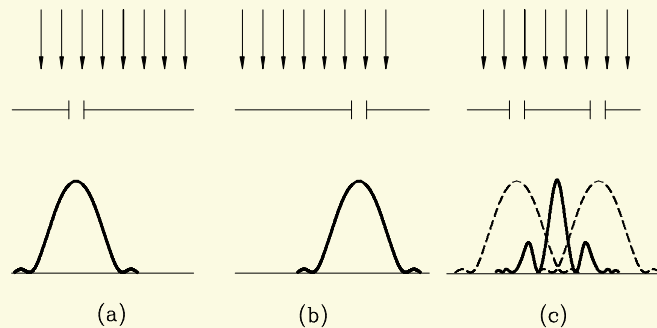
Localização de electrões: animação



5. Probabilidade de localização



$$P(x,t)dx = |\Psi(x,t)|^2 dx$$



$$|\Psi_{12}|^2 = |\Psi_1|^2 + |\Psi_2|^2 + 2Re(\Psi_1^* \Psi_2)$$